

Math 115

Summer 2017

Lecture 12



Simplify

$$\begin{aligned}
 1) \quad & (\underbrace{3.2}_{\text{blue}} \times 10^{23}) \cdot (\underbrace{4.5}_{\text{blue}} \times 10^{-40}) \\
 & = 14.4 \times 10^{-17} = 1.44 \times 10^1 \times 10^{-17} = \boxed{1.44 \times 10^{-16}}
 \end{aligned}$$

$$\begin{aligned}
 2) \quad & (-4x^5)^3 \cdot (-2x^7) = (-4)^3 (x^5)^3 \cdot (-2x^7) \\
 & = -64 x^{15} \cdot (-2x^7) \\
 & = \boxed{128 x^{22}}
 \end{aligned}$$

$$3) \left(\frac{-2x^7y^3}{3z^6} \right)^{-3} = \left(\frac{-2x^7}{3y^3z^6} \right)^{-3} = \left(\frac{3y^3z^6}{-2x^7} \right)^3$$

$$= \frac{27y^9z^{18}}{-8x^{21}} = \frac{-27y^9z^{18}}{8x^{21}}$$

$$4) (3x + 5)^2 \quad (A+B)^2$$

$$= (3x)^2 + 2(3x)(5) + (5)^2$$

$$= 9x^2 + 30x + 25$$

$$5) \frac{(-5x^6)^4}{(25x^8)^2} = \frac{(-5)^4 (x^6)^4}{25^2 (x^8)^2} = \frac{\cancel{625} x^{24}}{\cancel{625} x^{16}} = x^8$$

$$6) (4x^2 - 7)^2 = (4x^2)^2 - 2(4x^2)(7) + (7)^2$$

$$= 16x^4 - 56x^2 + 49$$

$$\textcircled{7} \quad \frac{12x^6 - 4x^3 + 8x}{-4x^2} = \frac{12x^6}{-4x^2} - \frac{4x^3}{-4x^2} + \frac{8x}{-4x^2}$$

$$= -3x^4 + x - \frac{2}{x}$$

$$\textcircled{8} \quad \frac{12x^3 - 5x^2 + x - 8}{x-1}$$

$$x \boxed{12x^2} = 12x^3$$

$$x \boxed{7x} = 7x^2$$

$$x \boxed{8} = 8x$$

$$\boxed{12x^2 + 7x + 8}$$

$$\begin{array}{r} 12x^2 + 7x + 8 \\ x-1 \overline{) 12x^3 - 5x^2 + x - 8} \\ \underline{-(12x^3 - 12x^2)} \\ 7x^2 + x - 8 \\ \underline{-(7x^2 - 7x)} \\ 8x - 8 \\ \underline{-(8x - 8)} \\ 0 \end{array}$$

$$\textcircled{9} \quad \underbrace{(5x^3 - 3y^2)(5x^3 + 3y^2)}_{\text{Conjugates}} = (5x^3)^2 - (3y^2)^2$$

Conjugates

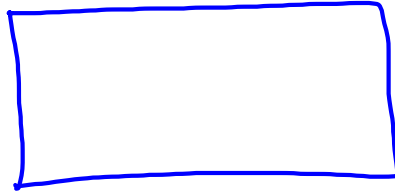
$$= \boxed{25x^6 - 9y^4}$$

$$\textcircled{10} \quad \frac{8.2 \times 10^{18}}{4.1 \times 10^{30}}$$

$$= 2 \times 10^{18-30}$$

$$= \boxed{2 \times 10^{-12}}$$

⑪



$$A = 15x^2 - 5x - 50$$

$$w = x - 2$$

Find L

$$\text{Hint } A = LW \Rightarrow L = \frac{A}{w}$$

$$\begin{array}{r} \overline{15x^2 - 5x - 50} \\ x-2 \overline{) 15x^2 - 5x - 50} \\ \underline{-(15x^2 - 30x)} \\ 25x - 50 \\ \underline{-(25x - 50)} \\ 0 \end{array}$$

$$L = 15x + 25$$

⑫ Give Deg. & Coef.

$$-24x^6y$$

$$C = -24, D = 6+1 = 7$$

⑬ Distribute & Simplify

$$\begin{aligned} & 6x^2(-5x + 4) - 10(x^3 + 5x^2 - 3x + 1) - 30x + 10 \\ &= -30x^3 + 24x^2 - 10x^3 - 50x^2 + 30x - 10 - 30x + 10 \\ &= \boxed{-40x^3 - 26x^2} \quad D=3, LC=-40 \end{aligned}$$

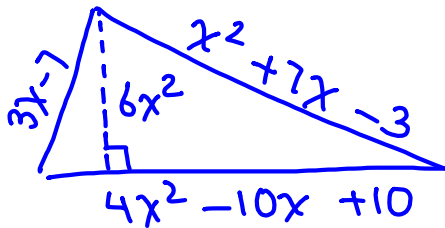
⑭ Foil & Simplify: $(2x-5)(4x^2+10x+25)+100$

$$= 8x^3 + 20x^2 + 50x - 20x^2 - 50x - 125 + 100$$

$$= \boxed{8x^3 - 25}$$

$$D=3, L.C.=8, \text{Const. } -25$$

find $A \in P$.



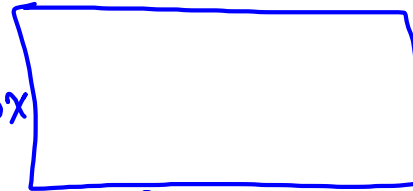
$$P = \underline{3x-7} + 4x^2 - \underline{10x+10} + \underline{x^2+7x-3}$$

$$P = 5x^2 \quad \text{Monomial} \quad D=2, C=5$$

$$A = \frac{3 \cancel{6} x^2 (4x^2 - 10x + 10)}{2}$$

$$A = 12x^4 - 30x^3 + 30x^2$$

$$8-5x$$



$$x^2 + 5x - 8$$

$$P = 2(x^2 + 5x - 8) + 2(8 - 5x)$$

$$P = 2x^2 \quad \begin{matrix} D=2 \\ C=2 \end{matrix}$$

$$A = (8-5x)(x^2+5x-8)$$

$$= 8x^2 + 40x - 64 - 5x^3 - 25x^2 + 40x$$

$$A = -5x^3 - 17x^2 + 80x - 64$$

Divide $\frac{6x^2 + 10x - 5}{3x - 1}$

$$\begin{array}{r} 2x \quad +4 \\ 3x-1 \overline{) 6x^2 + 10x - 5} \\ \underline{-(6x^2 - 2x)} \\ 12x \\ \underline{-(12x - 4)} \\ -1 \end{array}$$

$$3x \boxed{2x} = 6x^2$$

$$3x \boxed{4} = 12x$$

$$2x + 4 + \frac{-1}{3x-1}$$

Divide: $\frac{3x^3 - 5x^2 + 2}{x-1}$

$$x \boxed{} = 3x^3$$

$$x \boxed{} = -2x^2$$

$$x \boxed{} = -2x$$

$$3x^2 - 2x - 2$$

$$\begin{array}{r}
 3x^2 - 2x - 2 \\
 x-1 \overline{) 3x^3 - 5x^2 + 0x + 2} \\
 \underline{-(3x^3 - 3x^2)} \\
 -2x^2 + 0x + 2 \\
 \underline{-(-2x^2 + 2x)} \\
 -2x + 2 \\
 \underline{-(-2x + 2)} \\
 0
 \end{array}$$

Area of a rectangle is $4x^6 - 25$.
width is $2x^3 - 5$. Find its length.

$$2x^3 - 5 \overline{) 4x^6 - 25}$$

$$2x^3 \boxed{} = 4x^6 \quad \underline{-(4x^6 - 10x^3)} $$

$$2x^3 \boxed{} = 10x^3 \quad \underline{-(10x^3 - 25)} $$

$$L = 2x^3 + 5$$

$$\begin{array}{r}
 4x^6 - 25 \\
 \hline
 2x^3 - 5
 \end{array}$$

$$\frac{8x - 2}{2} = \frac{8x}{2} - \frac{2}{2} = 4x - 1$$

$$\frac{8x - 2}{2x} = \frac{8x}{2x} - \frac{2}{2x} = 4 - \frac{1}{x}$$

$$\frac{3x + 5}{5x - 3} \quad \text{Long Div. (Divide by Polynomial other than monomial)}$$

Exam III : Monday @ 6:00 AM

Ch. 5 : Factoring Polynomial

Writing a Polynomial in product form of other Polynomial is called factoring.

$$10x - 15 = \boxed{5} \cdot 2x - \boxed{5} \cdot 3$$


$$= \boxed{5(2x - 3)}$$

GCF

$$16x^3 + 12x^2 = \boxed{4x^2} \cdot 4x + \boxed{4x^2} \cdot 3$$


$$= 4x^2(4x + 3)$$

$$\begin{aligned}
 & 7x(3x+5) - 6(3x+5) \\
 &= (3x+5)(7x-6)
 \end{aligned}$$



$$25x^3y^2 - 10x^2y + 5xy$$

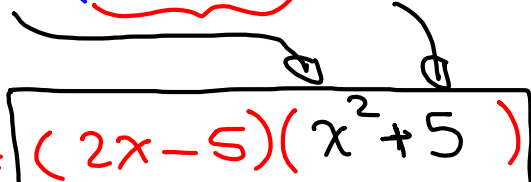
$$= 5xy(5x^2y - 2x + 1)$$



$$\begin{aligned}
 & 2x^3 - 5x^2 + 10x - 25 \\
 &= x^2(2x-5) + 5(2x-5)
 \end{aligned}$$

Grouping

$$= (2x-5)(x^2+5)$$



$$\begin{aligned}
 & 7x^3 + 3x^2 - 14x - 6 \\
 &= x^2(7x+3) - 2(7x+3) = (7x+3)(x^2-2)
 \end{aligned}$$

Factoring Trinomials $ax^2 + bx + c$

$$\begin{array}{lcl}
 x^2 + 10x + 24 & = & x^2 + 4x + 6x + 24 \\
 \swarrow \quad \uparrow & & \\
 P=24 & 1, 24 & \\
 S=10 & 2, 12 & \\
 & 3, 8 & \\
 & \textcircled{4, 6} & \\
 & & = (x+4)(x+6)
 \end{array}$$

$$\begin{array}{lcl}
 x^2 + x - 12 & = & x^2 - 3x + 4x - 12 \\
 \swarrow \quad \uparrow & & \\
 P=-12 & -1, 12 & \\
 S=1 & -2, 6 & \\
 & \textcircled{-3, 4} & \\
 & & = (x-3)(x+4)
 \end{array}$$

$$\begin{array}{lcl}
 2x^2 - 3x - 5 & = & 2x^2 + 2x - 5x - 5 \\
 \swarrow \quad \uparrow & & \\
 P=-10 & 1, -10 & \\
 S=-3 & \textcircled{2, -5} & \\
 & & = (x+1)(2x-5)
 \end{array}$$

$$\begin{array}{lcl}
 4x^2 + 5x - 9 & = & 4x^2 + 9x - 4x - 9 \\
 \swarrow \quad \uparrow & & \\
 P=-36 & -1, 36 & \\
 S=5 & -2, 18 & \\
 & -3, 12 & \\
 & \textcircled{-4, 9} & \\
 & -6, 6 & \\
 & & = (4x+9)(x-1)
 \end{array}$$

Special Factoring: Two Terms

$$A^2 + B^2 = \text{Prime}$$

$$A^2 - B^2 = (A + B)(A - B)$$

$$A^3 + B^3$$

$$A^3 - B^3$$

$$x^2 + 36 = x^2 + 6^2 \quad \text{Prime}$$

$$x^2 - 36 = x^2 - 6^2 = (x + 6)(x - 6)$$

$$4x^2 + 49 = (2x)^2 + 7^2 \Rightarrow \text{Prime}$$

$$4x^2 - 49 = (2x)^2 - 7^2 = (2x + 7)(2x - 7)$$

$$25x^2 + 64 = (5x)^2 + 8^2 \quad \text{Prime}$$

$$25x^2 - 64 = (5x)^2 - 8^2 = (5x + 8)(5x - 8)$$

Special Factoring: Two Terms

$$A^2 + B^2 = \text{Prime}$$

$$A^2 - B^2 = (A + B)(A - B)$$

$$A^3 + B^3 = (A + B)(A^2 - AB + B^2)$$

$$A^3 - B^3$$

$$x^3 + 125 = x^3 + 5^3$$

$$= (x + 5)(x^2 - 5x + 25)$$

$$27x^3 + 64 = (3x)^3 + (4)^3$$

$$= (3x + 4)(9x^2 - 12x + 16)$$

$$8x^3 + 27y^3 = (2x)^3 + (3y)^3$$

$$= (2x + 3y)(4x^2 - 6xy + 9y^2)$$

Special Factoring: Two Terms

$$A^2 + B^2 = \text{Prime}$$

$$A^2 - B^2 = (A + B)(A - B)$$

$$A^3 + B^3 = (A + B)(A^2 - AB + B^2)$$

$$A^3 - B^3 = (A - B)(A^2 + AB + B^2)$$


$$\begin{aligned} 125x^3 - 8 &= (5x)^3 - (2)^3 \\ &= (5x - 2)(25x^2 + 10x + 4) \end{aligned}$$

$$\begin{aligned} 1000x^3 - 27y^3 &= (10x)^3 - (3y)^3 \\ &= (10x - 3y)(100x^2 + 30xy + 9y^2) \end{aligned}$$

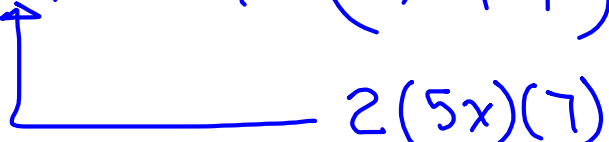
Special Factoring: Perfect-Square trinomials

$$A^2 + 2AB + B^2 = (A + B)^2$$


$$x^2 + 16x + 64 = (x + 8)^2$$



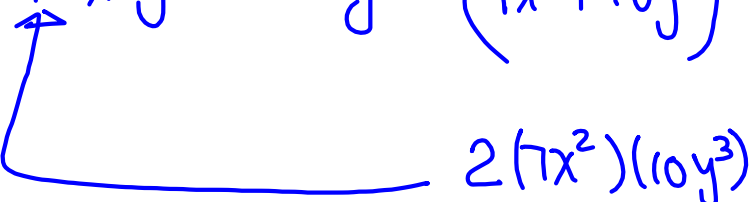
$$25x^2 + 70x + 49 = (5x + 7)^2$$



$$36x^2 + 60xy + 25y^2 = (6x + 5y)^2$$



$$49x^4 + 140x^2y^3 + 100y^6 = (7x^2 + 10y^3)^2$$



Special Factoring: Perfect-Square trinomials

$$A^2 - 2AB + B^2 = (A - B)^2$$

$$x^2 - 24x + 144 = (x - 12)^2$$

$$25x^2 - 60xy^5 + 36y^{10} = (5x - 6y^5)^2$$

$$x^2 - 13x + 36 = \cancel{(x - 6)^2}$$

$\swarrow \quad \searrow$
 $36 \quad P=36$
 $S=-13$

$$= \boxed{(x-9)(x-4)}$$